

1) If $4x - 7 = -9$, what is the value of $6x + 5$?

A 2

B 3

C 4

D 5

Sol: $4x - 7 = -9$; $x = -1/2$; $6x + 5 = 6(-1/2) + 5 = 2$

2) $x + 2y = 0$;
 $3x + y = -10$

The above system of equation is satisfied by which of the following ordered pairs?

A (2,-4)

B (-4,2)

C (-2, 4)

D (4,-2)

Sol: $x = -2y$; $3(-2y) + y = -10$; $-5y = -10$; $y = 2$; and $x = -4$;

$$S = 3000 + 3dc$$

3) A service company estimates the salary of any employee in dollars, using the above expression, where d is the number of days an employee works in a month and c is the total number of complaints he resolved in a month. Which of the following is the best interpretation of the number 3 in the expression?

- A** the company charges 3\$ per day for each of the complaint he resolves
B the minimum of 3 complaints are resolved per day
C the employee is paid 3 \$ everyday
D each day the employee works for 3 hours

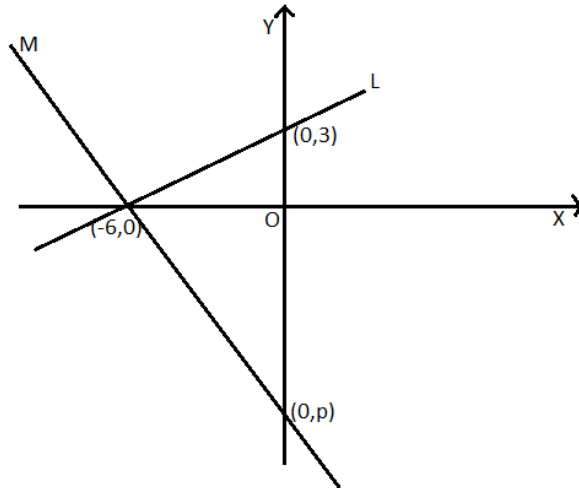
Sol: dc is the total number of complaints resolved in d days. the company charges 3\$ per day for each of the complaint he resolves.

- 4) $9a^4 - 30a^2b^3 + 25b^6$
A $(5a^2 - 3b^3)^2$
B $(3a^2 + 5b^3)^2$
C $(3a^2 - 5b^3)^2$
D $(3a - 5b)^4$

Sol: compare with the formula $(x - y)^2 = x^2 - 2xy + y^2$
 $x = 3a^2$ and $y = 5b^3$
 $(3a^2 - 5b^3)^2 = 9a^4 - 30a^2b^3 + 25b^6$

- 5) $\text{Sqrt}((x-1)^2 + 7) - k = 0$
If $x > 2$ and $k = 4$ in the equation above, what is the value of x ?
A 2
B 3
C 4
D 5

Sol: $\text{Sqrt}((x-1)^2 + 7) = 4$;
 $(x-1)^2 + 7 = 16$; $(x-1)^2 = 9$; $x-1 = 3$ or -3 ; $x = 4$ or -2 ;
Since $x > 2$ $x = 4$;



6) In the xy plane above, line l is perpendicular to line m and the two lines intersect on the x axis. What is the value of p?

- A -4
- B -6
- C -8
- D -12**

Sol: $(\frac{3}{6})(\frac{-p}{-6}) = -1$;
 $\frac{3p}{36} = -1$; $p = -12$

7) If $(x^a(a^2 + b^2))/(x^{2a}ab) = x^9$ and $a < 0$ and $b > 0$, what is the value of a-b?

- A -3**
- B 3
- C 9
- D -9

Sol: $x^a(a^2 + b^2 - 2ab) = x^9$;
 $(a-b)^2 = 9$; $a - b = 3$ Or -3 ;

Since $a < 0$ and $b > 0$ a-b is negative. So $a-b = -3$

$$R = 3n$$

- 8) The revenue R of an apple vendor is given by the above equation. n is the number of apples sold and R is the revenue. What should be the minimum number of an apples sold for the total revenue to be at least 100\$?

A 32

B 33

C 34

D 35

Sol: total revenue = $3n \geq 100$;

$$n \geq 100/3; \text{ min } p = 34$$

- 9) the line l in the xy plane has a slope 3 and passes through the point $(1,2)$ and the line m in the xy plane passes through the points $(2,3)$ and $(-2,2)$. If the y intercept of line l is a and the y intercept of line m is b then what is the value of $|a-b|$?

A $5/2$

B $7/2$

C $9/2$

D $11/2$

Sol: $y = 3x + c$; $(1,2)$ satisfies the equation; $2 = 3+c$; $c = -1=a$

$m = (3-2)/(2+2) = 1/4$; $y = x/4 + c$; $(2,3)$ satisfies the equation;

$$3 = 2/4 + c; c = 3 - 1/2 = 5/2=b$$

$$|a-b| = |-1-5/2| = 7/2$$

10) Which of the following equations has a graph in the xy plane for which y is always less or equal to 2?

A $y = -x^2 + 4$

B $y = -|x| + 3$

C $y = -(x+5)^2 + 1$

D $y = x^3 + 2$

Sol: $-(x+5)^2 < 0$; so $-(x+5)^2 + 1 < 1$; $y = -(x+5)^2 + 1$ always lies below 2.

11) Which of the following complex numbers is equivalent to $(1/3+4i) + (1/4-3i)$? (note : $i = \sqrt{-1}$)

A $(7-2i)/25$

B $(7+i)/25$

C $(7-i)/25$

D $(7+2i)/25$

Sol: $(1/3+4i) + (1/4-3i) = (3-4i)/25 + (4+3i)/25$;
 $(7-i)/25$

$$a = (v_f - v_i) / (t_f - t_i)$$

12) Acceleration (a) in the above formula is a measure of how quickly the velocity of the object changes. v_f is the final velocity and v_i is the initial velocity. t_f is the final time and t_i is the initial time. Which of the following expresses v_i in terms of other variables?

A $v_i = a(t_f - t_i) - v_f$

B $v_i = v_f - a(t_f - t_i)$

C $v_i = a(t_i - t_f) - v_f$

D $v_i = v_f - a(t_i - t_f)$

Sol: $a = (v_f - v_i) / (t_f - t_i)$; $(v_f - v_i) = a(t_f - t_i)$;
 $v_i = v_f - a(t_f - t_i)$

$$2x^2 - 16x + 24$$

- 13) If a and b are the solutions to the above equation, then what is the value of $1/a + 1/b$?

A $4/3$

B $3/4$

C $3/2$

D $2/3$

Sol: $1/a + 1/b = (a+b)/ab$;

$a + b = 16/2 = 8$; $ab = 24/2 = 12$

$(a+b)/ab = 8/12 = 2/3$

- 14) The amount of money in the saving account increases with an annual rate of 8 percent. If the initial amount in the savings account is 5000\$, which of the following functions f models the amount of money in the savings account, n years later?

A $5000(1.08)^n$

B $5000(.92)^n$

C $1.08(5000)^n$

D $.92(5000)^n$

Sol: every year money increases by a factor of 1.08. so after n years the money in the account is $5000(1.08)^n$

- 15) The expression $(3x^2 - 5x - 2)/(x - 2)$ is equivalent to which of the following?

A $3x - 1$

B $(3x + 1)/(x - 2)$

C $3x + 2$

D $3x + 1$

$$\text{Sol: } (3x^2 - 5x - 2)/(x-2) = (3x^2 - 6x + x - 2)/(x-2) = (3x(x-2) + (x-2))/(x-2) = 3x + 1;$$

- 16) A total of 60 grams of gold coins are awarded to the best employees of the company. Only 5 grams and 15 grams gold coins are given to the best employees. If at least one 5 gram and one 15 gram gold coins are awarded, what is one possible value of the number of 5 gram gold coins?

3,6,9

$$\text{Sol: } 5x + 15y = 60 ;$$

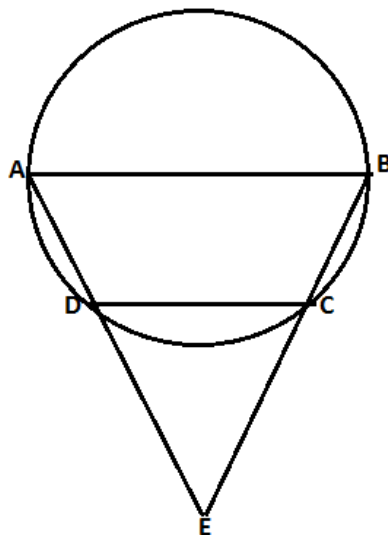
$x + 3y = 12$; since x and y are intergers, the possible solutions are $x = 3,6,9$ and $y = 3,2,1$.

- 17) $(x+5)(3x-1) = (a+b)x^2 + cx + (a-b)$
 a, b and c are constants in the above equation. If the equation is true for all values of x then what is the value of b ?

8

$$\text{Sol: } 3x^2 + 14x - 5 = (a+b)x^2 + cx + (a-b);$$

$$a+b = 3 \text{ and } a-b = -5; \Rightarrow b = 8;$$

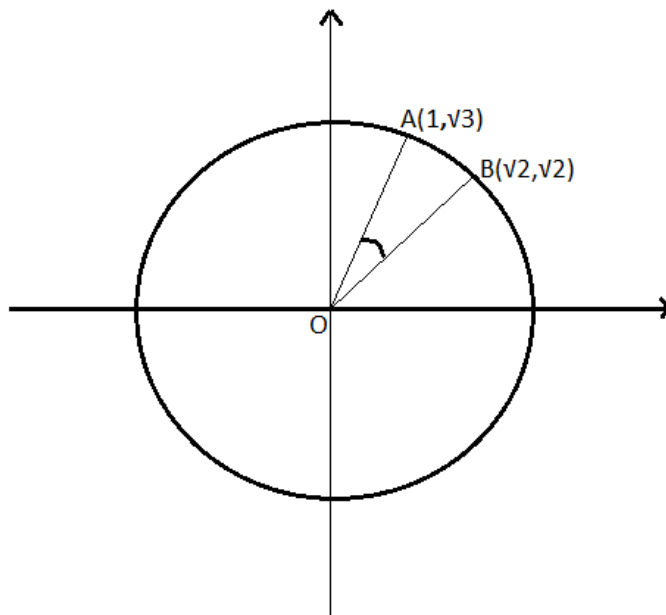


- 18) In the figure above, AB is the diameter of the circle. C and D are the midpoints of BE and AE respectively. If the radius of the circle is 6 cm then what is the value of CD?

6

Sol: ABE and DCE are similar triangles by SAS property. So $DC = \frac{1}{2}AB$.

$$DC = \frac{12}{2} = 6 \text{ cm.}$$



- 19) In the xy plane above, O is the center of the circle, and the measure of angle AOB is π/a radians. What is the value of a?

12

Sol: OB makes an angle of 45 degrees with x axis. And OA makes an angle of 60 degrees with x axis. So, angle AOB = 60-45 = 15 .

Angle AOB = $15(\pi/180) = \pi/12$. So, a = 12

$$6x + by + 8 = 0$$

$$2ax + 4y + 9 = 0$$

20) a and b are constants in the system of equations above. If the system of equations have zero solutions then what is the value of ab?

12

Sol: Since the equations have zero solutions , slopes are equal.

$$-6/b = -2a/4; ab = 12$$
